COURSE NAME: MPM2D – Principles of Mathematics	
Accumulative Activities: 10 **AS Learning: Topics: (1.1 to 4.6)** **Teacher: Antonio Pietrangelo**	**Student's Name:** **Student#:**
Time: Throughout Course	**Due Date: Tuesday, February 13th, 2024 2:30 pm EST**
Pages: 17, plus	**Mark:** /100

Categories	Knowledge/ Understanding	Thinking/Inquiry/ Problem Solving	Communication	Application
Symbol	K/U	T/I	C	A
Weight	25 %	25 %	25 %	25 %
Level	N/A	N/A	N/A	

Overall Expectations:

Expectations as listed in the Ontario Curriculum course outline for your specific course.

Specific Expectations:

Chapter/Unit 1 - Systems of Linear Equations
1.1 Representing Linear Relations
1.2 Solving Linear Equations
1.3 Graphically Solving Linear Systems
1.4 Solving Linear Systems: Substitution
1.5 Equivalent Linear Systems
1.6 Solving Linear Systems: Elimination
1.7 Exploring Linear Systems

Chapter 2: Analytic Geometry: Line Segments and Circles, and Advanced Shapes
2.1 Midpoint of a Line Segment
2.2 Length of a Line Segment
2.3 Equation of a Circle
2.4 Classifying Figures on a Coordinate Grid
2.5 Verifying Properties of Geometric Figures
2.6 Exploring Properties of Geometric Figures
2.7 Using Coordinates to Solve Problems

Chapter 3: Graphs of Quadratic
3.1 Exploring Quadratic Relations
3.2 Properties of Graphs of Quadratic Relations
3.3 Factored Form of a Quadratic Relation
3.4 Expanding Quadratic Expressions
3.5 Quadratic Models Using Factored Form
3.6 Exploring Quadratic and Exponential Graphs

Chapter 4: Factoring Algebraic
4.1 Common Factors in Polynomials
4.2 Exploring the Factorization of Trinomials
4.3 Factoring Quadratics: $x^2 + bx + c$, where $(a = 1)$
4.4 Factoring Quadratics: $x^2 + bx + c$, where $(a \neq 1)$
4.5 Factoring Quadratics: Special Cases
4.6 Reasoning about Factoring Polynomials

Rubrics:

Category	Level R (0 – 49%)	Level 1 (50-59%)	Level 2 (60-69%)	Level 3 (70-79%)	Level 4 (80-100%)	Level/ Mark
Knowledge – Understanding of **(Specific Expectations: 1.1 to 4.6 - Accumulative)**	**demonstrates insufficient understanding**	demonstrates limited understanding	demonstrates some understanding	demonstrates considerable understanding	demonstrates thorough understanding	
				Individual: Mark:		

Category	Level R (0 – 49%)	Level 1 (50-59%)	Level 2 (60-69%)	Level 3 (70-79%)	Level 4 (80-100%)	Level/ Mark
Thinking and Inquiry (What if scenarios) of: **(Specific Expectations: 1.1 to 4.6 - Accumulative)**	demonstrates insufficient ability to apply different scenarios	demonstrates limited ability to apply different scenarios	demonstrates some ability to apply different scenarios	demonstrates considerable ability to apply different scenarios	demonstrates through ability to apply different scenarios	
				Individual: Mark:		

Category	Level R (0 – 49%	Level 1 (50-59%)	Level 2 (60-69%)	Level 3 (70-79%)	Level 4 (80-100%)	Level/ Mark
Communication **Communicates effectively** **(Specific Expectations: 1.1 to 4.6 - Accumulative)**	demonstrates **insufficient** ability to communicate effectively	demonstrates **limited** ability to communicate effectively	demonstrates **some** ability to communicate effectively	demonstrates **considerable** ability to communicate effectively	demonstrates **through** ability to communicate effectively	
				Individual: Mark:		

Category	Level R (0 – 49%	Level 1 (50-59%)	Level 2 (60-69%)	Level 3 (70-79%)	Level 4 (80-100%)	Level/ Mark
Application: Demonstrates the ability to apply mathematical principles to real world situations. **(Specific Expectations: 1.1 to 4.6 - Accumulative)**	demonstrates **insufficient ability**	demonstrates **limited ability**	demonstrates **some ability**	demonstrates **considerable ability**	demonstrates **thorough ability**	
				Individual: Mark:		

PART A: KNOWLEDGE AND UNDERSTANDING (K/U) – 25% - 100%,
PART B: THINKING AND INQUIRY (T/I) - 25% to 100%, if implemented
PART C: COMMUNICATION (C) – 25 to 100%, if implemented
PART D: APPLICATION (A) – 25% to 100%, if implemented

Each activity will be out of 10 marks, and can be an assessment of one or more of PART A through D. The percentages will be adjusted depending on what sections have been implemented.

PART D: APPLICATION (A) – 100%

Activity 10: Factor these quadratic equations of the form y=ax²+bx+c, where a ≠ 1

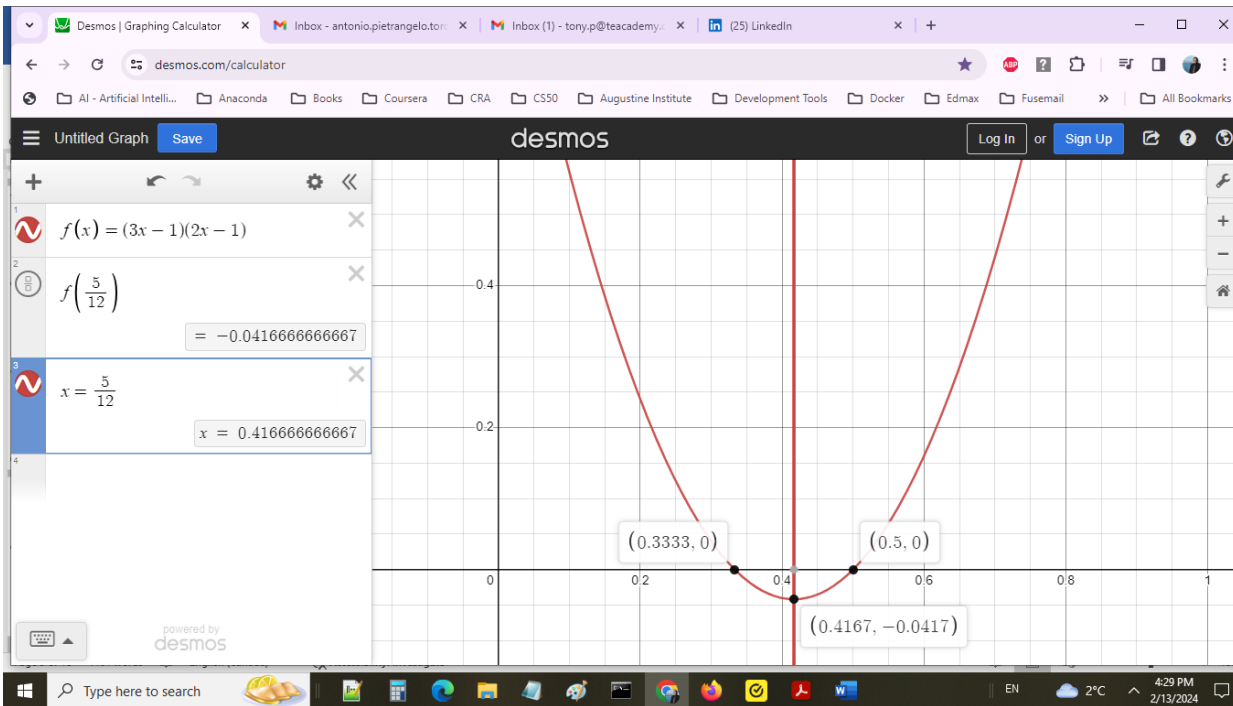For each quadratic equation find the following (Show all required details of work):

1. Find the factors, if possible and
2. Put the equation into factored form y = a(x – r)(x - s)
3. Find the axis of symmetry
4. Find the vertex of the parabola
5. Graph the equation using the details above

See example below for $6x^2 - 5x + 1$:

$6x^2 - 5x + 1$ $a = 6$ $b = -5$ $c = 1$	Factors $(a \times c) = 6$	Product	Sum (b) $b = a + c$	$=6x^2 - 5x + 1$ $=6x^2 - 2x - 3x + 1$ $=2x(3x - 1) - (3x - 1)$ $=(3x -1)(2x -1)$
	1, 6	6	7	Expand to prove:
	2, 3	6	5	$=(3x -1)(2x -1)$
	-1, -6	6	-7	$=6x^2 - 3x - 2x + 1$
	-2, -3	6	-5	$=6x^2 - 5x + 1$

Find axis of symmetry; occurs where y = 0	$y = (3x -1)(2x -1)$ $0 = (3x -1)(2x -1)$ Factor 1: $0 = (3x -1)$ <= Solve for x $-3x = -1$ $x_1 = \frac{-1}{-3} = \frac{1}{3}$ Factor 2: $0 = (2x -1)$ <= Solve for x $-2x = -1$ $x_2 = \frac{-1}{-2} = \frac{1}{2}$	$x_1 = r = \frac{1}{3} = 0.3334$ $x_2 = s = \frac{1}{2} = 0.50$ $x_S = \frac{(r+s)}{2} = \frac{\frac{1}{3}+\frac{1}{2}}{2}$ $x_S = \frac{\frac{2}{6}+\frac{3}{6}}{2}$ $x_S = \frac{5}{6} \times \frac{1}{2}$ $x_S = \frac{5}{12} = 0.4167$

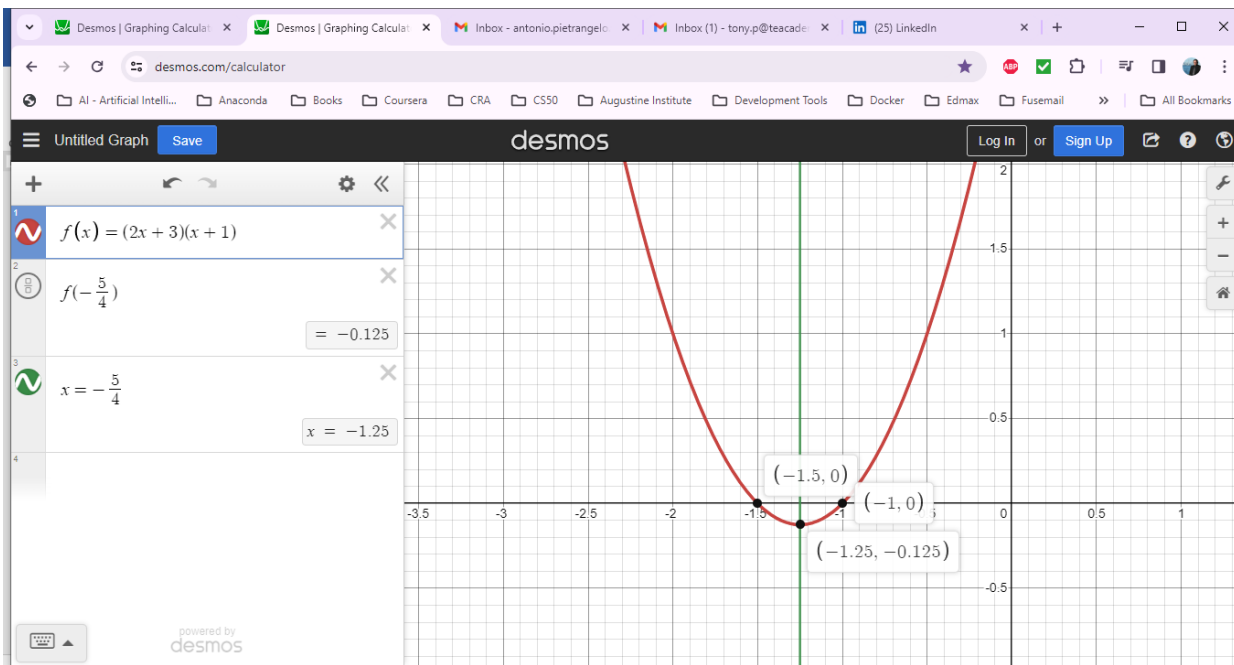|		
Find vertex $f(x_s)$, where x_s the axis of symmetry Vertex$(\frac{5}{12}, \frac{-1}{24})$	$Y = f(x_s) = (3x - 1)(2x - 1)$ $f(\frac{5}{12}) = (3(\frac{5}{12}) - 1)(2(\frac{5}{12}) - 1)$ $f(\frac{5}{12}) = ((\frac{15}{12} - \frac{12}{12})(\frac{10}{12} - \frac{12}{12})$	$f(\frac{5}{12}) = (\frac{3}{12})(\frac{-2}{12})$ $f(\frac{5}{12}) = (\frac{1}{4})(\frac{-1}{6}) = \frac{-1}{24}$ $y = f(\frac{5}{12}) = \frac{-1}{24} = -0.0417$

Graph of: $6x^2 - 5x + 1$

Continue with the following quadratic equations as per above

$2x^2 + 5x + 3$	Factors (a x c) = 6	Product	Sum (b) b = a + c	$=2x^2 + 5x + 3$
	1, 6	12	7	$=2x^2 + 2x + 3x + 3$ $=2x(x + 1) + 3(x + 1)$ $=(x + 1)(2x + 3)$
a = 2 b = 5 c = 3	2, 3	12	5	Expand to prove: $=(x + 1)(2x + 3)$ $=2x^2 + 3x + 2x + 3$ $=2x^2 + 5x + 3$

Find axis of symmetry; occurs where y = 0	$y = (x + 1)(2x + 3)$ $y = (2x + 3)(x + 1)$ $0 = (2x + 3)(x + 1)$ Factor 1: $0 = (2x + 3)$ $-2x = 3$ $x_1 = -\frac{3}{2}$ Factor 2: $0 = (x + 1)$ $x_2 = -1$	$x_1 = r = -\frac{3}{2} = -1.5$ Type equation here. $x_2 = s = -1$ $x_S = \frac{(r+s)}{2} = \frac{\frac{-3}{2}+\frac{-2}{2}}{2}$ $x_S = \frac{\frac{-5}{2}}{2}$ $x_S = \frac{-5}{2} \times \frac{1}{2}$ $x_S = \frac{-5}{4}$

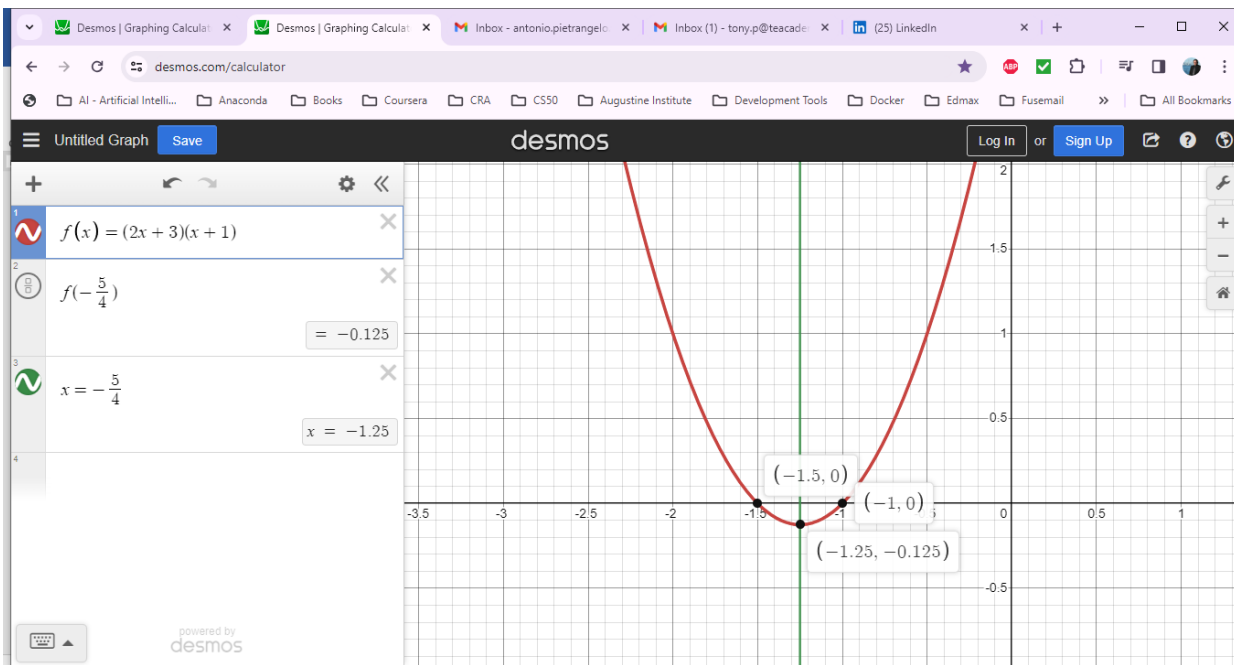| Find vertex $f(x_s)$, where x_s the axis of symmetry Vertex (x_s, y)	$Y = f(x_s) = (2x + 3)(x + 1)$ $f(\frac{-5}{4}) = (2(\frac{-5}{4}) + 3)(\frac{-5}{4} + 1)$ $f(\frac{-5}{4}) = (\frac{-10}{4} + \frac{12}{4})(\frac{-5}{4} + \frac{4}{4}) = (\frac{2}{4})(\frac{-1}{4})$ $f(\frac{-5}{4}) = \frac{-1}{8} = -0.125$	Vertex$(x, y) = (\frac{-5}{4}, \frac{-1}{8})$

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Graph of: $y = 2x^2 + 5x + 3$; $y = (2x + 3)(x + 1)$

Continue with the following quadratic equations as per above

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$2x^2 + 5x + 3$

a = 2
b = 5
c = 3

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Factors (a x c) = 6	Product	Sum (b) b = a + c
1, 6	6	7
2, 3	6	5

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$=2x^2 + 5x + 3$
$=2x^2 + 2x + 3x + 3$
$=2x(x + 1) + 3(x + 1)$
$=(x + 1)(2x + 3)$

Expand to prove:
$=(x + 1)(2x + 3)$
$=2x^2 + 3x + 2x + 3$
$=2x^2 + 5x + 3$

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Find axis of symmetry; occurs where y = 0

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y = (x + 1)(2x + 3)
y = (2x + 3) (x + 1)
0 = (2x + 3) (x + 1)

Factor 1:
$0 = (2x + 3)$
$-2x = 3$
$x_1 = -\dfrac{3}{2}$

Factor 2:
$0 = (x + 1)$
$x_2 = -1$

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$x_1 = r = -\dfrac{3}{2}$

Type equation here.

$x_2 = s = -1$

$x_S = \dfrac{(r+s)}{2} = \dfrac{\frac{-3}{2}+\frac{-2}{2}}{2}$

$x_S = \dfrac{\frac{-5}{2}}{2}$

$x_S = \dfrac{-5}{2} \times \dfrac{1}{2}$

$x_S = \dfrac{-5}{4}$

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Find vertex $f(x_s)$, where x_s the axis of symmetry

Vertex (x_s, y)

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$Y=f(x_s) = (2x + 3) (x + 1)$

$f(\frac{-5}{4}) = (2(\frac{-5}{4}) +3)(\frac{-5}{4} + 1)$

$f(\frac{-5}{4}) = (\frac{-10}{4}+ \frac{12}{4})(\frac{-5}{4} + \frac{4}{4}) = (\frac{2}{4})(\frac{-1}{4})$

$f(\frac{-5}{4}) = \frac{-1}{8} = -0.125$

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Vertex(x, y) = $(\frac{-5}{4}, \frac{-1}{8})$

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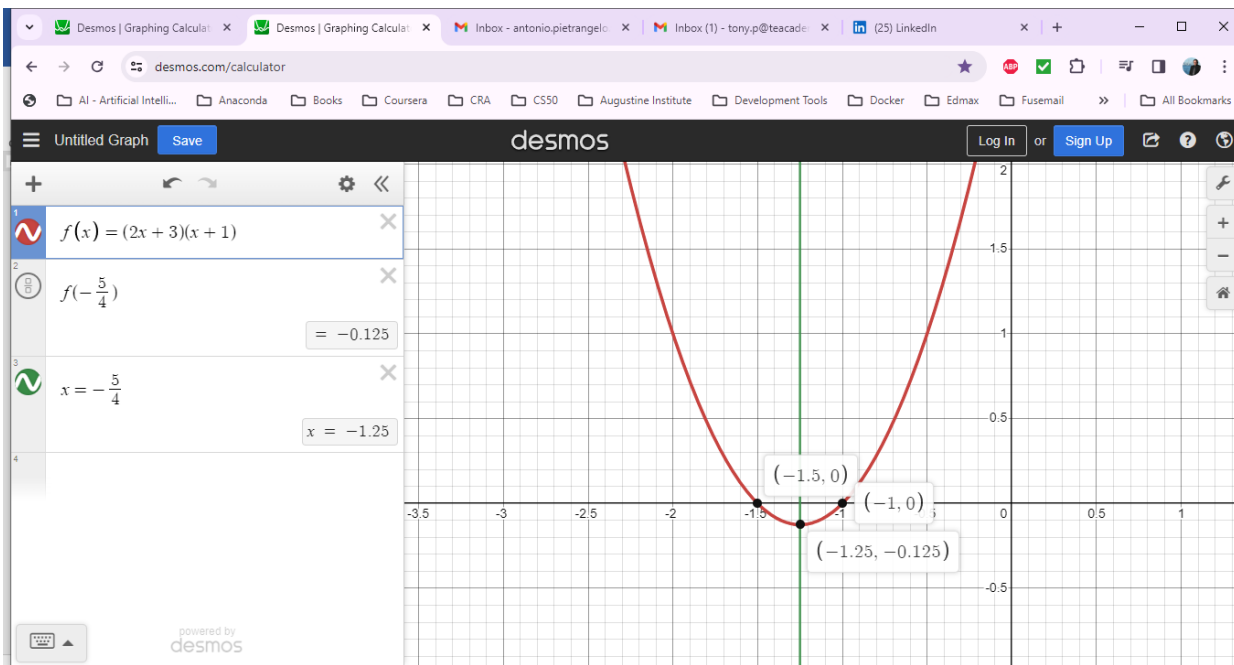</table>

Graph of: $y = 2x^2 + 5x + 3$; $y = (2x + 3)(x + 1)$

$3x^2 + 7x + 4$		
$6x^2 + 5x + 1$		
$6x^2 + 11x + 1$		
$2x^2 + 7x + 5$		
$6y^2 + 19y + 8$		
$12q^2 + 17q + 6$		

Continue with the following quadratic equations as per above

$3x^2 + 7x + 4$ a = 3 b = 7 c = 4	Factors (a x c) = 12	Product	Sum (b) b = a + c	=$2x^2$ + 5x + 3 =$2x^2$ + 2x + 3x + 3 =2x(x + 1) + 3(x + 1) =(x + 1)(2x + 3) Expand to prove: =(x + 1)(2x + 3) =$2x^2$ + 3x + 2x + 3 =$2x^2$ + 5x + 3
	1, 12	12	13	
	2, 6	12	5	

Find axis of symmetry; occurs where y = 0	Y=(x + 1)(2x + 3) y = (2x + 3) (x + 1) 0 = (2x + 3) (x + 1) Factor 1: 0 = (2x + 3) -2x = 3 x_1 = - $\frac{3}{2}$ Factor 2: 0 = (x + 1) x_2 = -1	x_1 = r = - $\frac{3}{2}$ Type equation here. x_2 = s = -1 $x_S = \frac{(r+s)}{2} = \frac{\frac{-3}{2}+\frac{-2}{2}}{2}$ $x_S = \frac{\frac{-5}{2}}{2}$ $x_S = \frac{-5}{2}$ x $\frac{1}{2}$ $x_S = \frac{-5}{4}$

Find vertex $f(x_s)$, where x_s the axis of symmetry Vertex (x_s, y)	Y=f(x_s) = (2x + 3) (x + 1) $f(\frac{-5}{4}) = (2(\frac{-5}{4}) +3)(\frac{-5}{4} + 1)$ $f(\frac{-5}{4}) = (\frac{-10}{4}+ \frac{12}{4})(\frac{-5}{4} + \frac{4}{4}) = (\frac{2}{4})(\frac{-1}{4})$ $f(\frac{-5}{4}) = \frac{-1}{8}$ = - 0.125	Vertex(x, y) = $(\frac{-5}{4}, \frac{-1}{8})$

Graph of: $y = 2x^2 + 5x + 3$; $y = (2x + 3)(x + 1)$

THANK YOU!!!