

VECTORS

Chapter 8 –Equations of Lines and Planes

(Material adapted from Chapter 8 of your text)

$A\infty\Omega$
MATH@TD

Chapter 8 – Equations of Lines and Planes

Contents with suggested problems from the Nelson Textbook (Chapter 8)

8.1 Vector and Parametric Equations of a Line in $\mathbb{R}^2$ – Pg. 157 – 161

Pg. 432 Investigation (smile as you do it)

Pg. 433 – 434 #1 – 3, 5, 6, 9 – 12

8.2 Cartesian and Symmetric Equations of Lines – Pg 162 – 165

Pg. 442 Investigation (whistle a happy tune)

Pg. 443 – 444 #1 – 3, 5 – 7, 9, 10, 12

8.3 Lines in Three Space – Pg 166 – 167

KNOW the equations for line in 3-Space

Pg. 449 – 450 #1, 2, 4 – 6, 8 – 11

8.4 Vector and Parametric Equations of Planes – Pg. 168 – 170

Read Example 4 on Pg. 458

Pg. 459 – 460 #3, 4, 6, 7 (beautiful), 9 – 11, 13

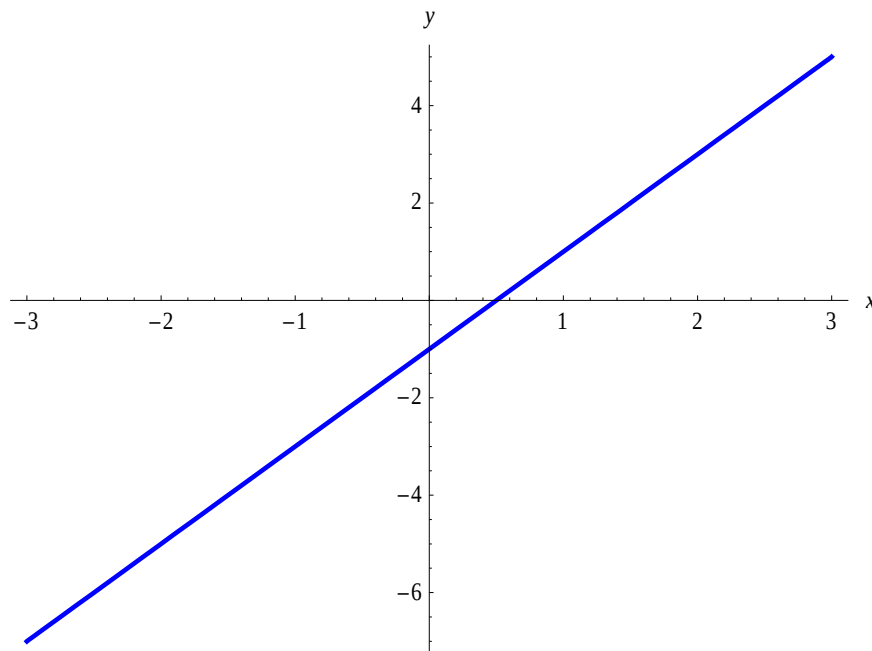
8.5 The Cartesian Equation of a Plane – Pg. 171 – 173

Pg. 468 – 469 #1, 2, 4 – 6, 8 – 11

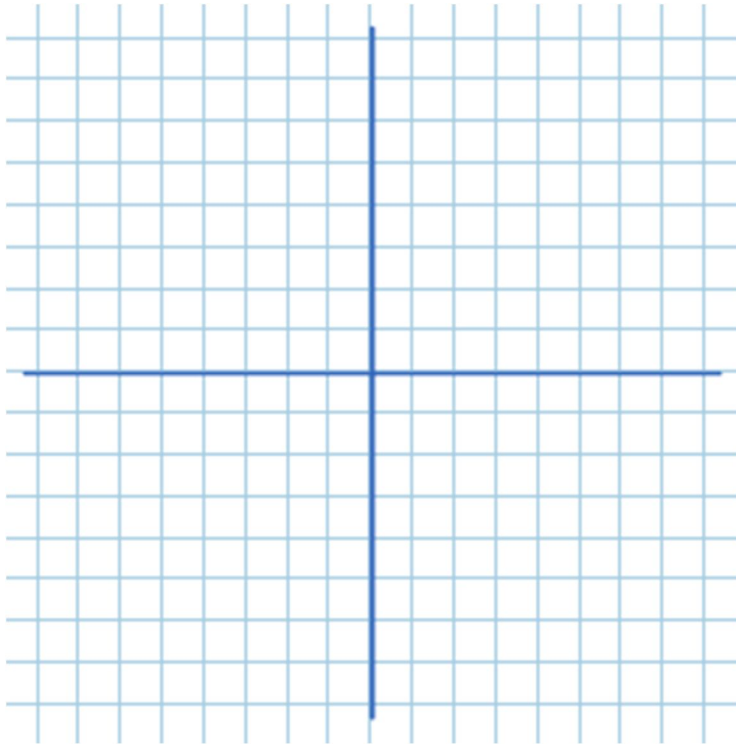
8.1 Vector and Parametric Equations of Lines (1)

Recall: A line is a **set of points** $\{(x, y) \mid y = mx + b\}$ where $y = mx + b$ is a functional relationship between domain and range values.

Consider the sketch of $y = 2x - 1$:

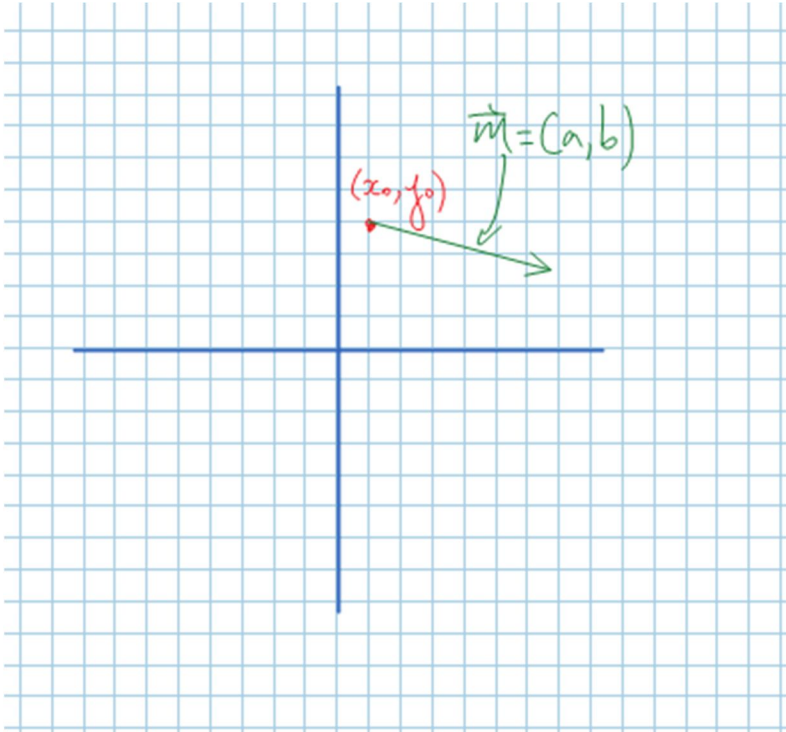


Problem: Consider a line with a direction vector $\vec{m} = (1, 2)$



Vector Equation of a Line

Consider the sketch of a line through the **known** point (x_0, y_0) with **direction vector** $\vec{m} = (a, b)$.



Example 8.1.1

Determine a vector equation of the line through $A(-1, 4)$ with direction $\vec{m} = (4, 1)$.

We can also write this as:

Note:

Q. Is the point $B(5, 9)$ on our line?

Q. Is the vector equation of a line **unique**?

Example 8.1.2

Obtain a vector equation (and parametric equations) for the line passing through the points $A(2, 5)$ and $B(-1, 2)$.

Example 8.1.3

Determine vector and parametric equations for the line through $A(-1, 3)$ and which is perpendicular to the line with vector equation $\vec{r} = (2, 1) + t(-2, 3)$.

Class/Homework for Section 8.1

Pg. 432 Investigation (smile as you do it)

Pg. 433 – 434 #1 – 3, 5, 6, 9 – 12